

# Population-level control of heterologous protein production in bacteria

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Imperial College  
London

CSynBI  
Centre for Synthetic Biology and Innovation

If we want to ...

We have to fight with ...

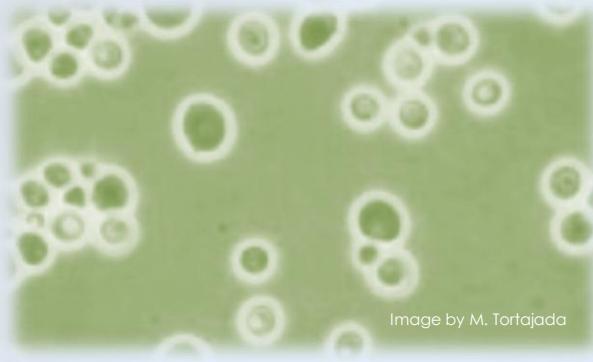


Image by M. Tortajada

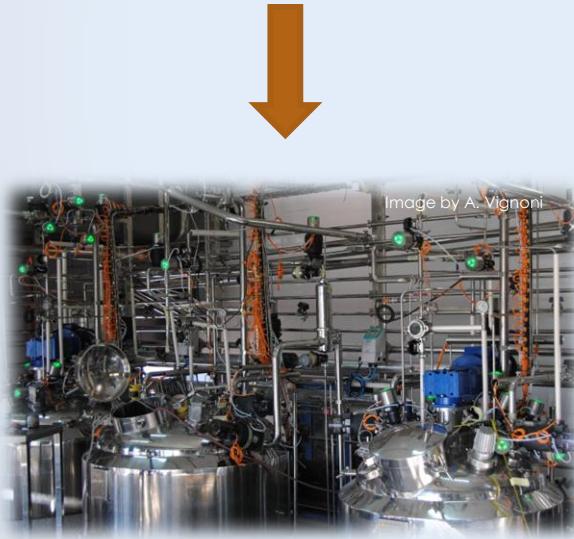
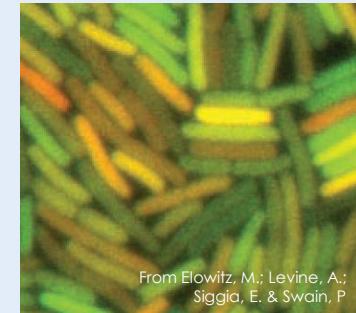


Image by A. Vignoni

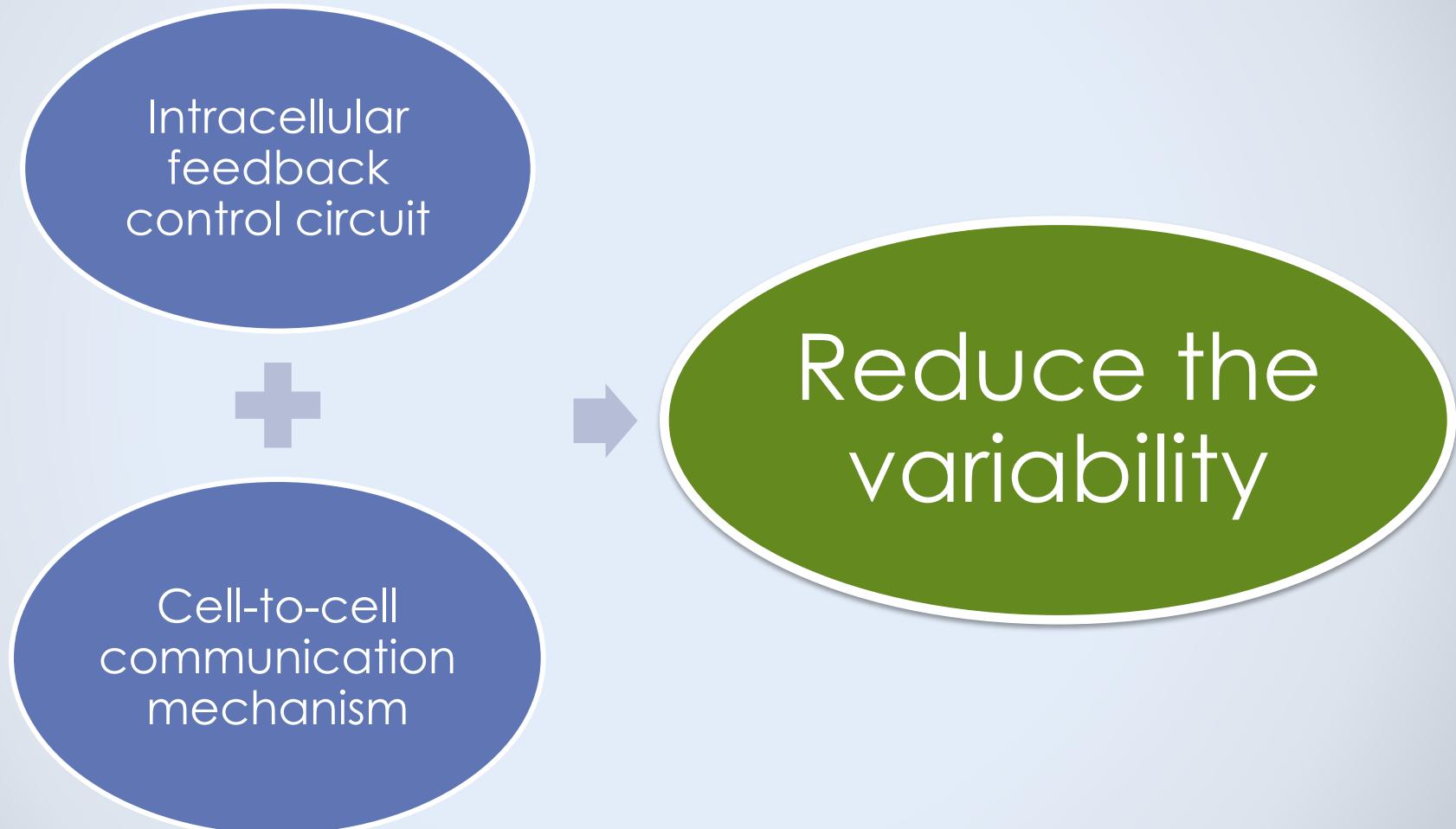
Variability in  
gene expression.



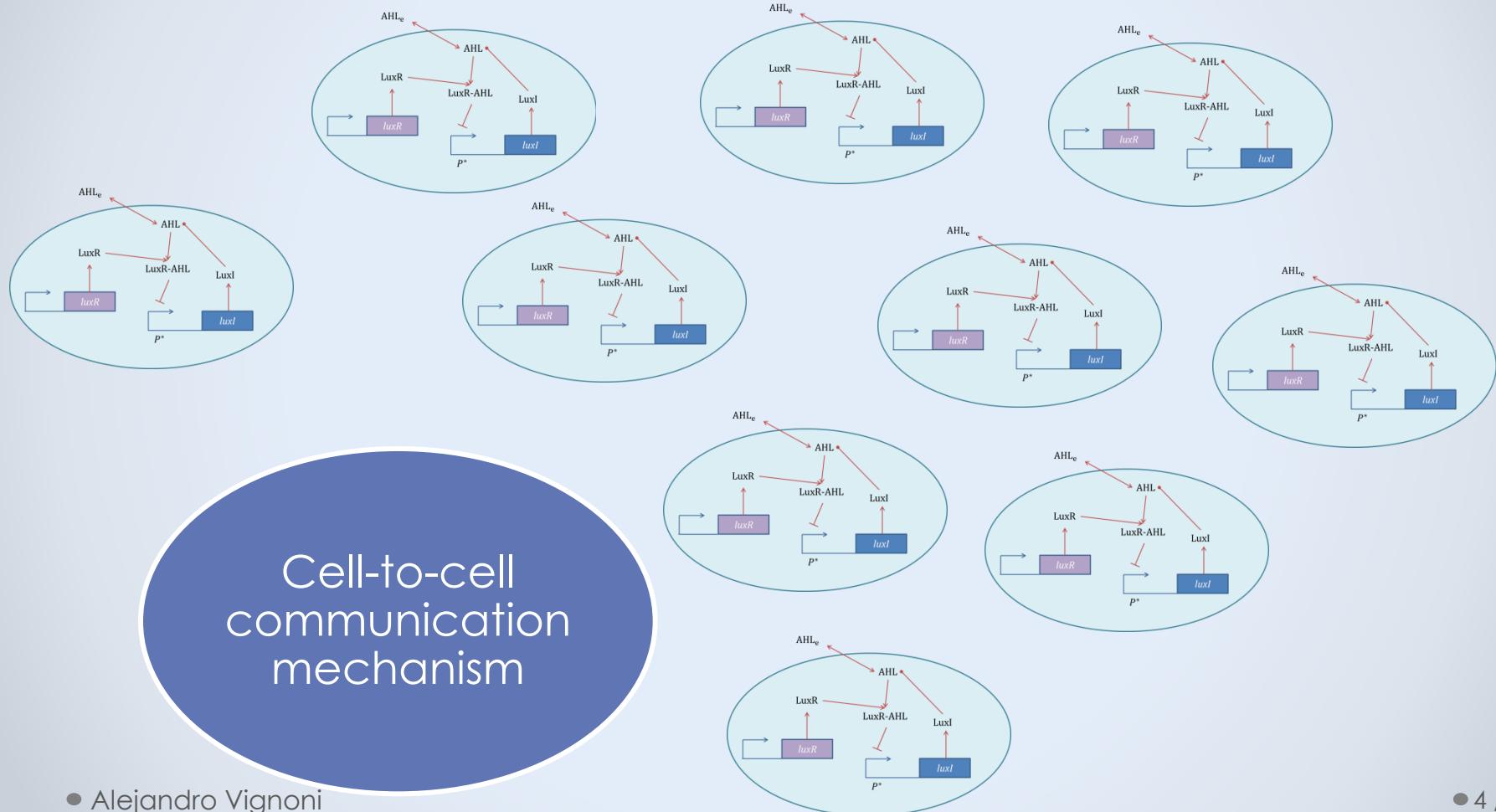
From Elowitz, M.; Levine, A.; Siggia, E. & Swain, P

How?

# Using a synthetic gene network

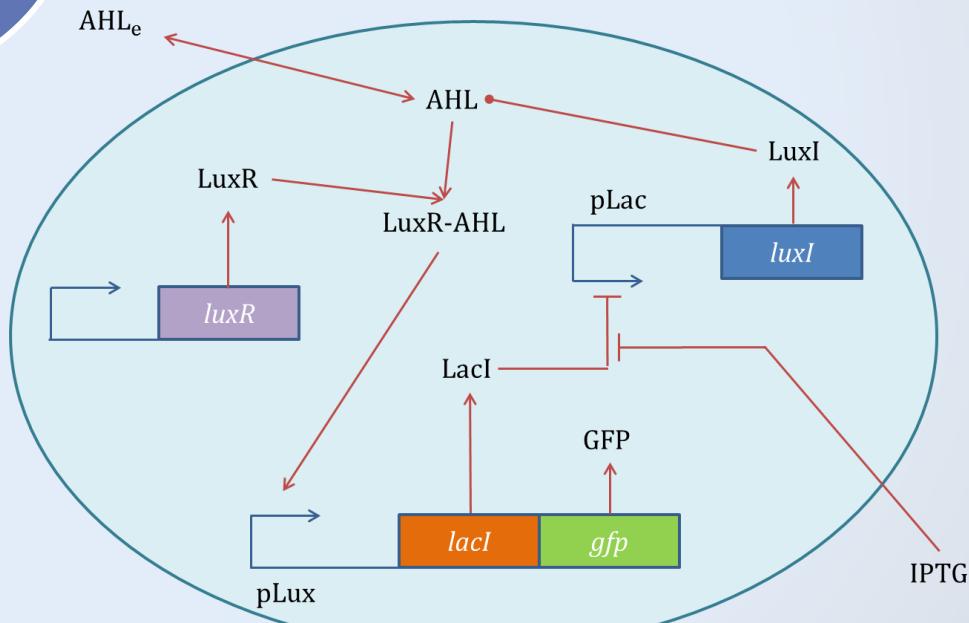


# Using a synthetic gene network

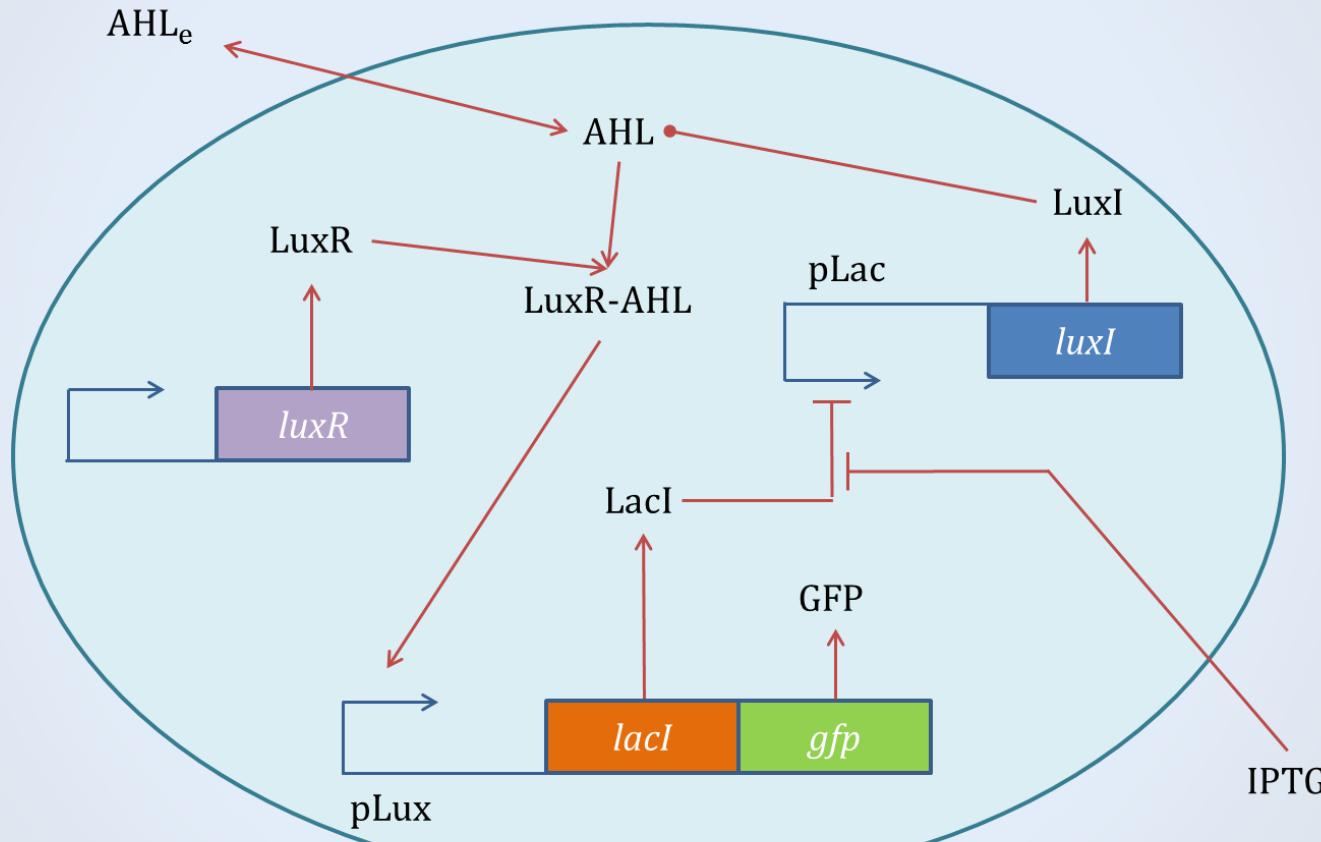


# Using a synthetic gene network

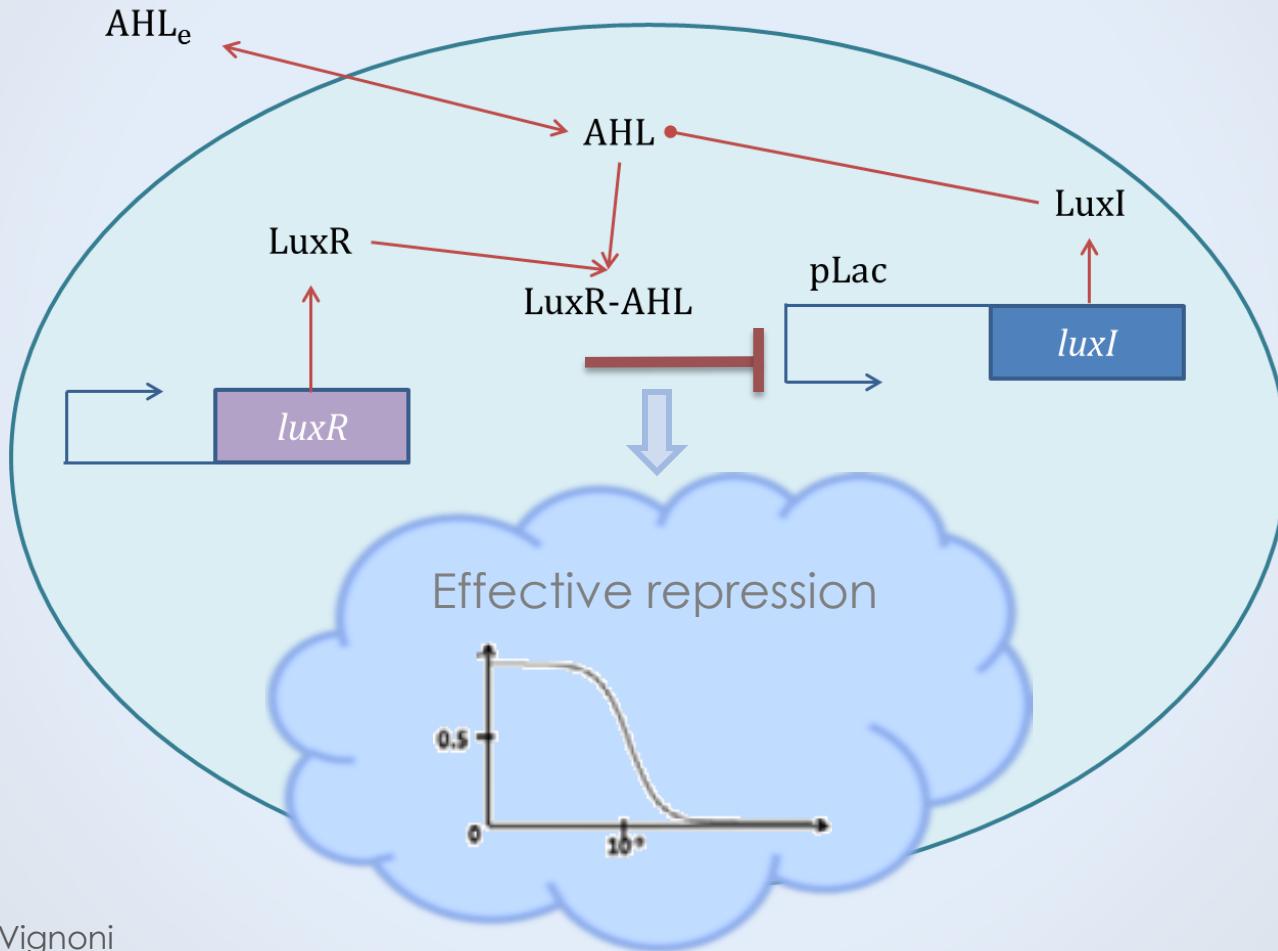
Intracellular  
feedback  
control circuit



# Genetic circuit

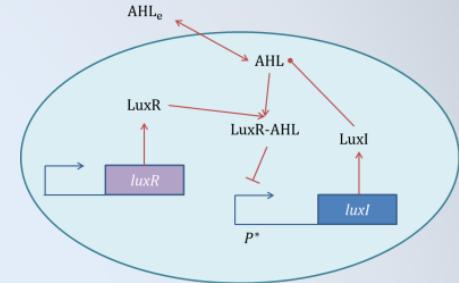


# Genetic circuit – Mathematical model



# Let's see the **model** of our genetic circuit.

$$Cell_i: \begin{cases} \frac{d[LuxI]_i}{dt} = b_i + u([AHL]_i) - \gamma_I [LuxI]_i \\ \frac{d[AHL]_i}{dt} = K_A [LuxI]_i + d([AHL]_i - [AHL]_e) - \gamma_A [AHL]_i \end{cases}$$



$b_i$	→ Basal expression of <i>LuxI</i>	$K_A$	→ AHL synthesis rate.
$u([AHL]_i)$	→ effective repressor hill function	$d$	→ Membrane permeability
$\gamma_I$	→ <i>LuxI</i> degradation rate	$\gamma_A$	→ AHL degradation rate

$$External AHL dynamic \quad \frac{d[AHL]_e}{dt} = \frac{d_e}{N} \sum_i^N ([AHL]_i - [AHL]_e) - \gamma_{Ae} [AHL]_e$$

$K_A$	→ AHL synthesis rate.	$\gamma_{Ae}$	→ External AHL decay rate
$d_e$	→ External membrane permeability	$N$	→ Number of cells

# The effective Hill function: the key element of the model

$$u([AHL]_i)_{hill} = \frac{K_I / K_h^\eta}{1 + ([AHL]_i / K_h)^\eta}$$

$\eta$  Hill coefficient

$K_h$  Half concentration constant

$K_I$  Dynamic range

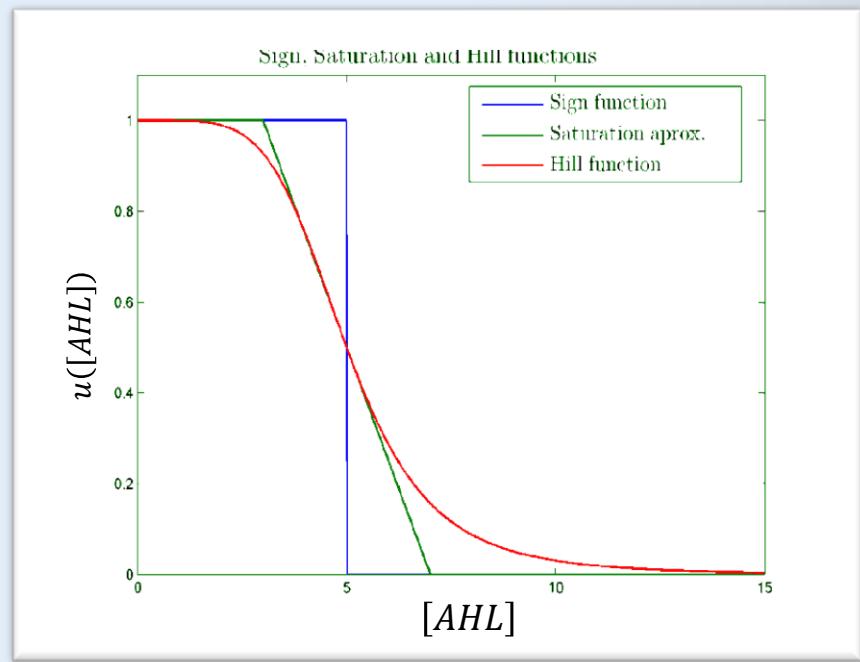


*Control Parameters*

**S** Slope

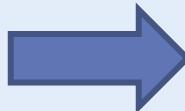
**T** Threshold

**R** Range



For analytical purposes:  
Saturation Approximation.

Theoretical analysis  
and  
mathematical model



$$\text{Var}\{[AHL]\} = f_V(S, T)$$

$$\mathbb{E}\{[AHL]\} = f_E(S, T, R)$$

Mean and variance  
can be controlled  
independently

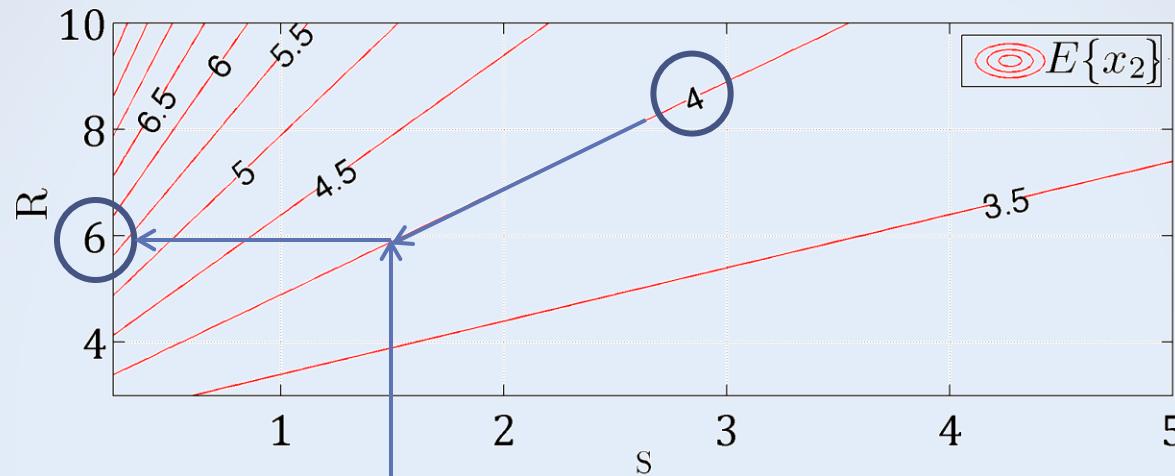
We will select the genetic regulation control parameters.



To obtain the desired gene expression variability distribution.

We obtain a R-S chart for the Mean and the Variance

R-S chart of  $x_2$  mean and variance

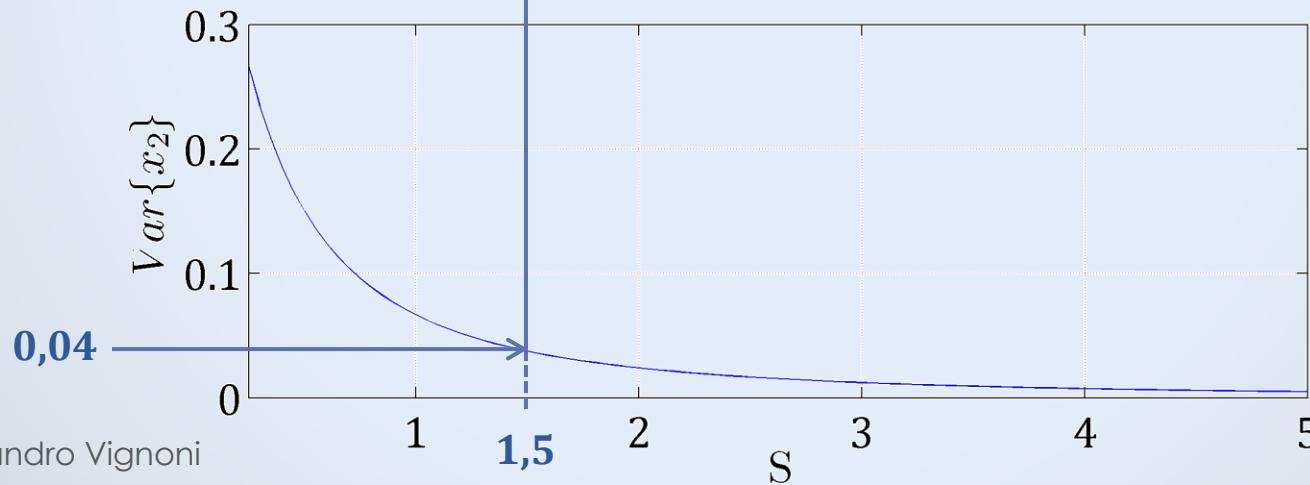


If we want

Mean: 4

Variance: 0,04

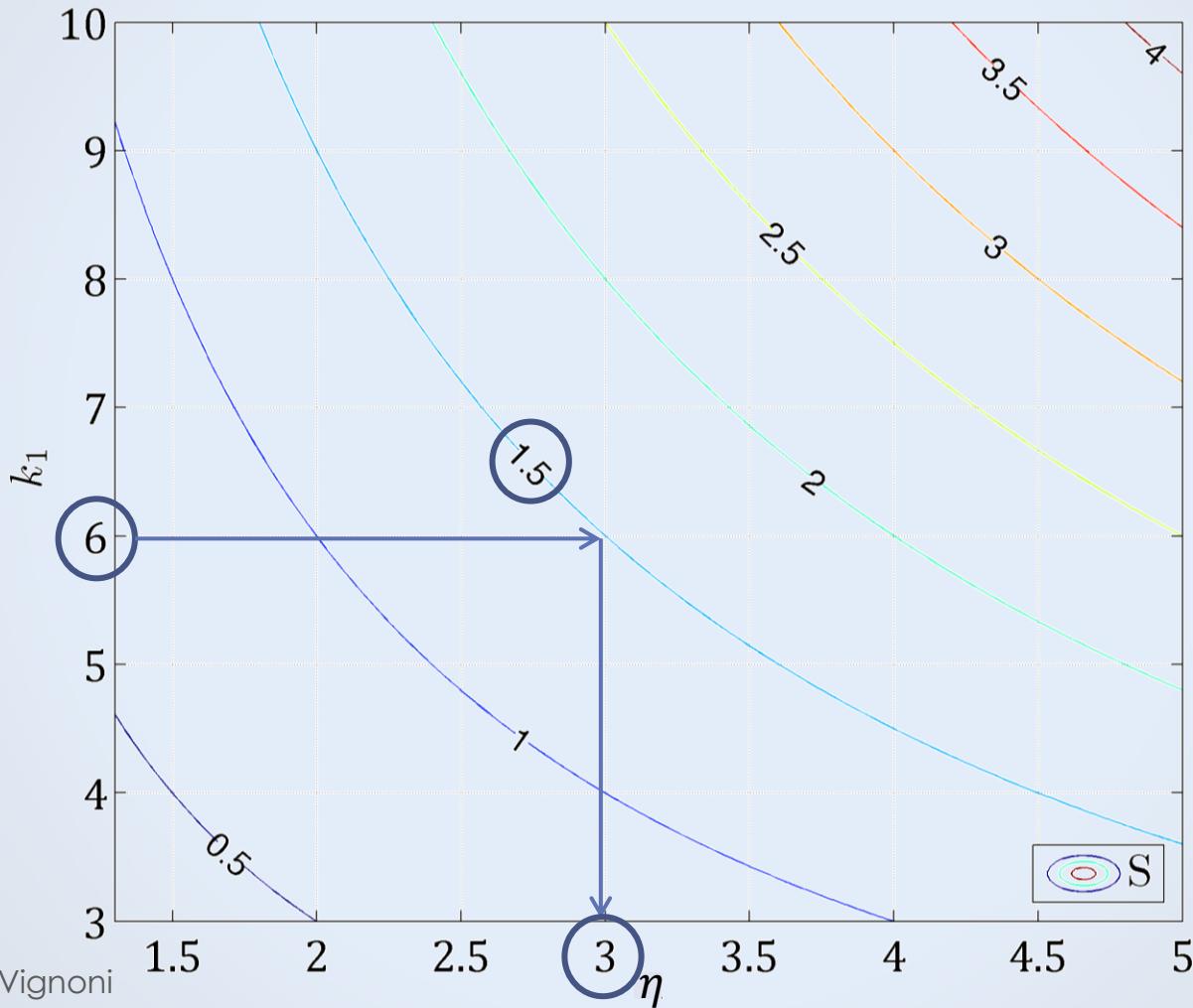
For a fixed  $T$



# Chart of control parameters

From the previous chart

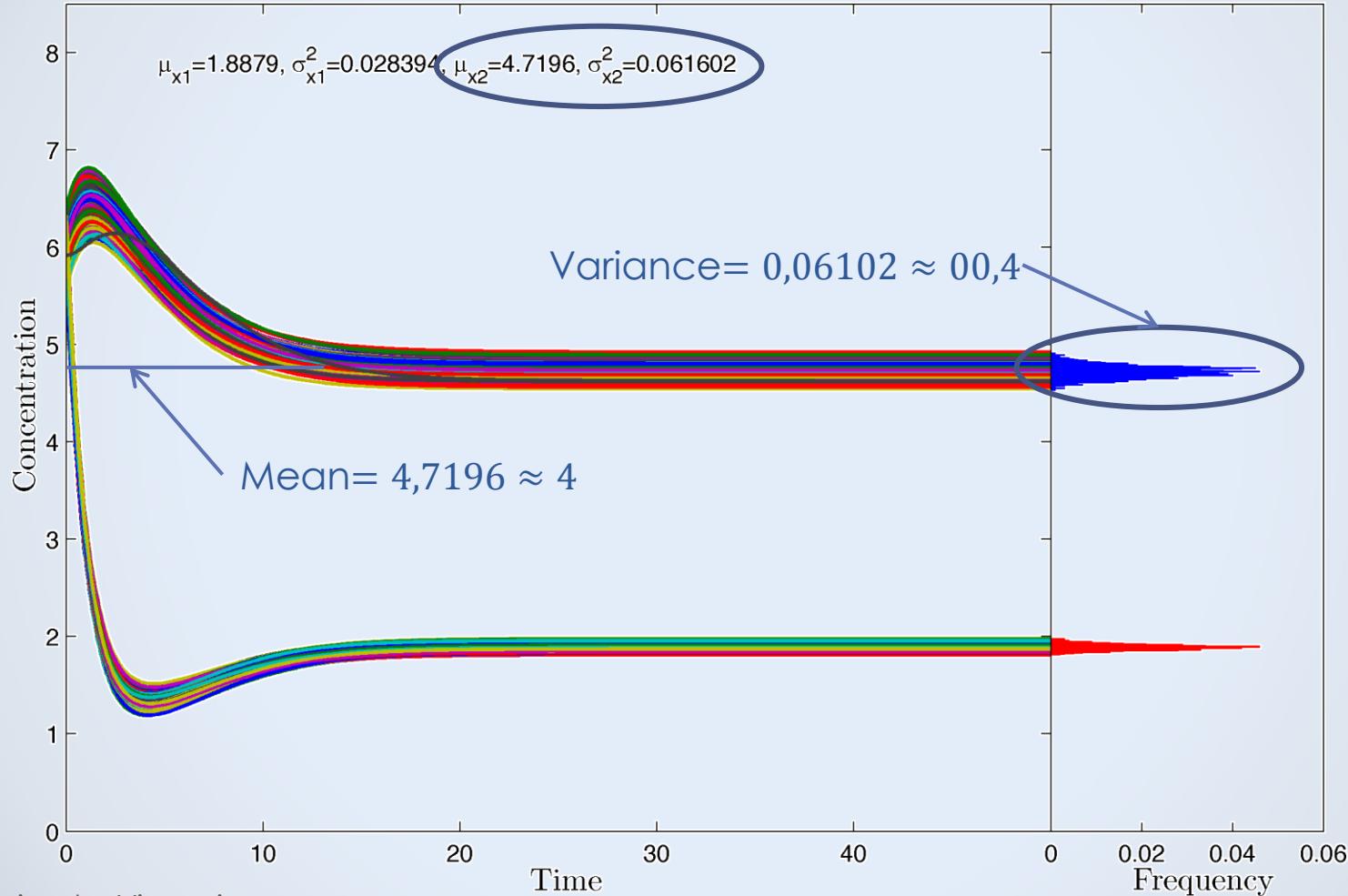
- $R=k_1=6$
- $S=1,5$



We obtain

- $k_1=6$
- $\eta=3$

We perform a ***simulation experiment*** introducing more stochasticity



# Summary

- **Control** of the *mean* and the *variance* of the gene expression noise *can be done*.
- Parameters chart to help the design
- Simulation experiments
- Synthetic biology potential for industrial applications.

# Future work

- Improve the model
- Make Experiments: Which parameters can we tune ?

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